

$$Y(\omega) = \frac{1}{Z(\omega)} = \frac{1}{\frac{1}{j\omega C_1} + \frac{1}{j\omega C_2 + \frac{1}{R_L}}}$$

$$Y(\omega) = \frac{1}{\frac{1}{j\omega C_1} + \frac{R_L}{j\omega C_2 R_L + 1}} = \frac{(j\omega C_1)(j\omega C_2 R_L + 1)}{j\omega C_2 R_L + 1 + j\omega C_2 R_L} = \frac{j\omega C_1 - \omega^2 C_1 C_2 R_L}{1 + j\omega R_L (C_1 + C_2)}$$

$$Y(\omega) = \left(\frac{j\omega C_1 - \omega^2 C_1 C_2 R_L}{1 + j\omega R_L (C_1 + C_2)} \right) \left(\frac{1 - j\omega R_L (C_1 + C_2)}{1 - j\omega R_L (C_1 + C_2)} \right) = \frac{(j\omega C_1 - \omega^2 C_1 C_2 R_L)(1 - j\omega R_L (C_1 + C_2))}{1 + \omega^2 R_L^2 (C_1 + C_2)^2}$$

$$Y(\omega) = \frac{j\omega C_1 + \omega^2 R_L C_1 (C_1 + C_2) - \omega^2 C_1 C_2 R_L + j\omega^3 R_L^2 C_1 C_2 (C_1 + C_2)}{1 + \omega^2 R_L^2 (C_1 + C_2)^2}$$

$$Y(\omega) = \frac{\omega^2 R_L C_1 (C_1 + C_2) - \omega^2 C_1 C_2 R_L}{1 + \omega^2 R_L^2 (C_1 + C_2)^2} + \frac{j\omega C_1 + j\omega^3 R_L^2 C_1 C_2 (C_1 + C_2)}{1 + \omega^2 R_L^2 (C_1 + C_2)^2}$$

$$Y(\omega) = \frac{\omega^2 R_L C_1 (C_1 + C_2 - C_2)}{1 + \omega^2 R_L^2 (C_1 + C_2)^2} + j\omega C_1 \frac{1 + \omega^2 R_L^2 C_2 (C_1 + C_2)}{1 + \omega^2 R_L^2 (C_1 + C_2)^2}$$

Asumiendo:

$$\omega^2 R_L^2 (C_1 + C_2)^2 \gg 1$$

como consecuencia tenemos que:

$$\omega^2 R_L^2 (C_1 + C_2) \gg \gg 1$$

$$\text{Porque } (C_1 + C_2) > (C_1 + C_2)^2$$

$$\text{Para } 0 < (C_1 + C_2) < 1$$

Entonces despreciando los 1

$$Y(\omega) = \frac{\omega^2 R_L C_1^2}{\omega^2 R_L^2 (C_1 + C_2)^2} + j\omega C_1 \frac{\omega^2 R_L^2 C_2 (C_1 + C_2)}{\omega^2 R_L^2 (C_1 + C_2)^2}$$

$$Y(\omega) = \frac{C_1^2}{R_L (C_1 + C_2)^2} + j\omega C_1 \frac{C_2}{(C_1 + C_2)}$$

$$Y(\omega) = \frac{C_1^2}{R_L (C_1 + C_2)^2} + j\omega \frac{C_1 C_2}{C_1 + C_2} = \frac{1}{R_L \left(\frac{C_1 + C_2}{C_1} \right)^2} + j\omega \frac{C_1 C_2}{C_1 + C_2}$$

Y por lo tanto

$$R_p = R_L \left(\frac{C_1 + C_2}{C_1} \right)^2 \text{ y } C_p = \frac{C_1 C_2}{C_1 + C_2}$$